

A New Approach of Functional Dependency in a Neutrosophic Relational Database Model

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Abstract -In order to model the imprecise and uncertain information, different classical relational data model have been studied in literature using vague set theory. However, neutrosophic set, as a generalized vague set, has more powerful ability to process fuzzy information than vague set. In this paper, we have proposed a neutrosophic relational database model and have defined a new kind of neutrosophic functional dependency (called α -nfd) based on the α -equality of tuples and the similarity measure of neutrosophic sets. Next, we present a set of sound neutrosophic inference rules which are similar to Armstrong's axioms for the classical case. Finally, partial α -nfd and neutrosophic key have been studied with the new notion of α -nfd and also tested.

Keywords: Neutro-sophic Set, Similarity Measure of Neutrosophic Data, Neutro-sophic Functional Dependency (α -Nfd), Partial α -Nfd, Neutro-sophic Key

I. INTRODUCTION

Real world information is very often imprecise in nature. Neutrosophic set theory, introduced by Smarandache in 2001 [I] has been widely used in literature [VIII, IX, X, IV, XI] to incorporate such imprecise data into classical relational databases. However, vague set theory was put forward by Gau and Buehrer [XVI] in 1993 as a more efficient tool to deal with uncertain data. A vague set, conceived as a generalization of the concept of fuzzy set, is a set of objects each of which has a grade of membership whose value is a continuous sub-interval of [0,1].

A vague set V which is characterized by a truth membership function t_v and a false membership function f_v where $t_v + f_v \leq 1$. In vague set certain portion i.e., $(1-t_v + f_v)$ is still undeterministic and also affect on taking decision. Now neutrosophic set has been introduced to deal with imprecise information in a more efficient manner than vague set theory using truth membership function t_v , indeterminacy membership function i_v , and a false membership function f_v . And the extended database model is then called a neutrosophic database model. However, compared to fuzzy and vague databases, much less research has been reported so far in the literature of neutrosophic database. Since data dependencies play an important role in any database design so, objective of this paper is to design the concepts of functional dependencies on neutrosophic database called neutrosophic functional dependency (α -nfd). The concept of α -nfd is

defined based on similarity measure of neutrosophic data which is again a new concept defined by the authors in this paper. This paper is organized as follows. Section 2 presents some basic knowledge about the neutrosophic set theory. Basic neutrosophic database concept is reported in section 3. In this section we also introduce new concepts of similarity measure of neutrosophic data, α -equality of neutrosophic data, neutrosophic functional dependencies (α -nfd) between two sets of attributes. The said concepts are then used to define Armstrong's axioms and other inference rules, neutrosophic partial functional dependency and neutrosophic key. Finally in Section 4 we draw an overall conclusion of the work.

II. BASICS OF NEUTROSOPHIC SET

In this section, we introduce the new concept of neutrosophic set. Let U be the universe of discourse where an element of U is denoted by u .

Definition 1: A neutrosophic set X on the universe of discourse U is characterized by three membership functions given by:

1. a truth membership function $t_x : U \rightarrow [0,1]$,
2. a false membership function $f_x : U \rightarrow [0,1]$ and
3. an indeterminacy membership function $i_x : U \rightarrow [0,1]$ such that $t_x(a) + f_x(a) \leq 1$ and $t_x(a) + f_x(a) + i_x(a) \leq 2$ and is written as $X = \{ \langle x, [t_x(a), i_x(a), f_x(a)] \rangle, a \in U \}$.

Definition 2: A Neutrosophic set 'N' is an empty neutrosophic set, denoted by ϕ , if and only if its truth-membership function $t_n(u) = 0$, indeterminacy-membership function $i_n(u) = 0$ and false-membership function $f_n(u) = 1$ for all u on U .

Definition 3: A Neutrosophic set 'A' is contained in another neutrosophic set 'B', written as $A \subseteq B$, if and only if, $t_A \leq t_B, i_A \leq i_B$ and $f_A \geq f_B$.

Definition 4: Two Neutrosophic sets 'A' and 'B' are equal, written as $A = B$, iff, $A \subseteq B$ and $B \subseteq A$, that is, $t_A = t_B, i_A = i_B$ and $f_A = f_B$.

Definition 5:The union of two neutrosophic sets A and B is a neutrosophic set C , denoted as $C = A \cup B$, whose truth-membership, indeterminacy-membership and false-membership functions are related to those of A and B by $t_C = \max(t_A, t_B)$, $i_C = \min(i_A, i_B)$ and $f_C = \min(f_A, f_B)$.

Definition 6:The intersection of two Neutrosophic sets A and B is a neutrosophic set C , written as $C = A \cap B$, such that $t_C = \min(t_A, t_B)$, $i_C = \max(i_A, i_B)$ and $f_C = \max(f_A, f_B)$.

III. NEUTROSOPHIC RELATIONAL DATABASE MODEL

Here, we make an attempt to extend the classical relational database model to incorporate neutrosophic data by means of neutrosophic set theory, which results in the Neutrosophic Relational Database model (NRDB).

TABLE I NEUTROSOPHIC RELATIONAL INSTANCE OF DE-QUERVAIN’S DISEASE RELATION

Name	Age	UricAcid(UA)	LiquidChromatography(LC)
Asmith	30	{6.5 <.92,.01,.03> }	{6.9 <.94,.01,.02> }
Bell	22	{7 <.99,.0015,.01> }	{6.5 <.99,.012,.01> }
Jackson	45	{7.35 <.9,.02,.04> }	{6.8 <.95,.01,.01> }
Bisop	33	{3.23 <.71,.026,.12> }	{7.5 <.80,.015,.14> }
Ritesh	40	{7.1 <.98,.01,.01> }	{8.1 <.74,.125,.22> }
Pradip	58	{6.85 <.913,.012,.03> }	{6.3 <.96,.02,.01> }
Amlesh	60	{7.25 <.97,.01,.02> }	{7.4 <.85,.015,.04> }
Nisitha	52	{6.4 <.90,.02,.03> }	{5.9 <.91,.01,.06> }
Madhumita	35	{5.7 <.76,.01,.22> }	{6.4 <.98,.001,.02> }
Neha	43	{7.15 <.98,.001,.01> }	{6.65 <.97,.02,.03> }

Example 1: Consider the neutrosophic relational instance r over De-Quervain’s Disease relation (NAME, UricAcid, LiquidChromatography) given above in Table 1. In r , UricAcid and LiquidChromatography are neutrosophic attributes. The first tuple in r means the employee with NAME = “Asmith” has the uric acid of {6.5, <.92,.01,.03>} and the LiquidChromatography of {6.9, <.94,.01,.02>}, which are neutrosophic sets. Here the neutrosophic data {6.5, <.92,.01,.03>} means the evidence in favour of “The uric acid is 6.5” is .92, the indeterminacy part .01 and the evidence against it is .03 and so on.

A. Similarity Measure of Neutrosophic Data

There have been some studies in literature which discuss the topic concerning how to measure the degree of similarity between vague sets [II, III, V, VI, VII]. This similarity measure did not fit well in some cases. We have introduced a new similarity measure between neutrosophic sets [XII, XIII, XIV, XV] which turned out to be more reasonable in more general cases which have been used in the present work which is defined as follows:

Definition 1:Let x and y be any two neutrosophic values such that $x = [t_x, i_x, f_x]$ and $y = [t_y, i_y, f_y]$ where

$$0 \leq t_x \leq 1, 0 \leq i_x \leq 1, 0 \leq f_x \leq 1 \text{ and } 0 \leq t_y \leq 1, 0 \leq i_y \leq 1, 0 \leq f_y \leq 1$$

$$\text{with } 0 \leq t_x + f_x \leq 1, 0 \leq t_y + f_y \leq 1, 0 \leq t_x + i_x + f_x \leq 2,$$

$$0 \leq t_y + i_y + f_y \leq 2$$

Now the similarity measure between two neutrosophic data denoted by $SE(x, y)$ is defined as follows

$$SE(x,y) = \sqrt[3]{1 - \frac{|(t_x - t_y) - (i_x - i_y) - (f_x - f_y)|}{3} (1 - |(t_x - t_y) + (i_x - i_y) + (f_x - f_y)|)}$$

B. Neutrosophic Functional Dependency

In this paper, similar to classical functional dependency, we define a new notion of neutrosophic functional dependency (called α -nfd) based on the concept of α -equality of neutrosophic tuples which plays important role in designing neutrosophic database. Next, we present a set of neutrosophic inference rules which are similar to Armstrong’s axioms for the classical case.

Definition 2:Let $r(R)$ be a neutrosophic relation on the relational schema $R(A_1, A_2, \dots, A_n)$. Let t_1 and t_2 be any two neutrosophic tuples in r . Let $\alpha \in [0, 1]$ be a threshold or choice parameter, predefined by the database designer, and $X = \{A_1, A_2, \dots, A_k\} \subseteq R$. Then the neutrosophic tuples t_1 and t_2 are said to be α -equal on X if $SE(t_1[A_i], t_2[A_i]) \geq \alpha \forall i = 1, 2, 3, \dots, k$. We denote this equality by the notation $t_1[X](NE)_\alpha t_2[X]$. The following proposition is straightforward from the above definition.

Proposition 1:If $0 \leq \alpha_2 \leq \alpha_1 \leq 1$, then

$$t_1[X](NE)_{\alpha_1} t_2[X] \Rightarrow t_1[X](NE)_{\alpha_2} t_2[X]$$

Definition 3:Let $X, Y \subset R = \{A_1, A_2, \dots, A_n\}$. Choose a threshold value $\alpha \in [0, 1]$. Then a neutrosophic functional dependency (α -nfd), denoted by $X \xrightarrow[\alpha]{nfd} Y$ is said to exist

if, whenever $t_1[X](NE)_\alpha t_2[X]$, it is also the case that $t_1[Y](NE)_\alpha t_2[Y]$. It may be read as “ X neutrosophic functionally determines Y at α -level”. In another way, “ Y is neutrosophic functionally determined by X at α -level”. The following proposition for α -nfd is straightforward.

Proposition 2: If $0 \leq \alpha_2 \leq \alpha_1 \leq 1$, then

$$X \xrightarrow[\alpha_1]{nfd} Y \Rightarrow X \xrightarrow[\alpha_2]{nfd} Y$$

Example 2: Consider the neutrosophic relational instance r presented in Table 1. Let us check whether $UA \xrightarrow[\alpha]{nfd} LC$, holds to a certain α -level of choice or not. Using the Definition 3.1 we have calculated $SE(t_p[UA], t_q[UA])$ and $SE(t_p[LC], t_q[LC])$ for every pair of tuples t_p and t_q and the results are shown below in Table 2 and Table 3 respectively.

TABLE II SIMILARITY MEASURE FOR UA

	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
t ₁	1	.93	.99	.89	.95	.99	.97	.99	.93	.97
t ₂	.93	1	.97	.91	.99	.98	.99	.98	.93	.99
t ₃	.99	.97	1	.9	.96	.99	.96	.99	.93	.88
t ₄	.89	.91	.9	1	.86	.92	.87	.81	.93	.86
t ₅	.95	.99	.96	.86	1	.96	.99	.96	.92	.99
t ₆	.99	.98	.99	.92	.96	1	.97	.99	.94	.97
t ₇	.97	.99	.96	.87	.99	.97	1	.96	.77	.99
t ₈	.99	.98	1	.81	.96	.99	.96	1	.93	.96
t ₉	.93	.93	.93	.93	.92	.94	.77	.93	1	.92
t ₁₀	.97	.99	.88	.86	.99	.97	.99	.96	.92	1

TABLE III SIMILARITY MEASURE FOR LC

	t ₁	t ₂	t ₃	t ₄	t ₅	t ₆	t ₇	t ₈	t ₉	t ₁₀
t ₁	1	.96	.99	.95	.85	.98	.94	.98	.97	.96
t ₂	.96	1	.97	.87	.86	.98	.91	.96	.99	.98
t ₃	.99	.97	1	.94	.85	.99	.94	.97	.98	.97
t ₄	.95	.87	.94	1	.89	.97	.96	.95	.92	.93
t ₅	.85	.86	.85	.89	1	.86	.84	.86	.87	.88
t ₆	.98	.98	.99	.97	.86	1	.93	.98	.99	.98
t ₇	.94	.91	.94	.96	.84	.93	1	.95	.93	.92
t ₈	.98	.96	.97	.95	.86	.98	.95	1	.97	.96
t ₉	.97	.99	.98	.92	.87	.99	.93	.97	1	.98
t ₁₀	.96	.98	.97	.93	.88	.98	.92	.96	.98	1

For $\alpha = 0.8$ (given by decision maker), we can see from the above two tables, that for any pair of tuples t_p & t_q if $SE(t_p[UA], t_q[UA]) \geq \alpha$ then it is also the case that $SE(t_p[LC], t_q[LC]) \geq \alpha$

So, we can say that the α -nfd $UA \xrightarrow[\alpha]{nfd} LC$ holds for the neutrosophic relational instance r . Also, from above Table 2

and Table III, we can say that the α -nfd $UA \xrightarrow[\alpha]{nfd} LC$ holds. However the α -nfd $UA \xrightarrow[\alpha]{nfd} LC$ does not hold because for tuples t_4 and t_2 , $SE(t_4[UA], t_2[UA]) = 0.91 \geq 0.9$, but $SE(t_4[LC], t_2[LC]) = 0.87 \leq 0.9$.

C. Inference Rules for α -nfd

It is well known that in classical relational databases, functional dependencies satisfy a set of inference rules called Armstrong’s axioms. In this section, we have derived a set of inference rules for our proposed α -nfd. These neutrosophic inference rules are similar to Armstrong’s axioms for functional dependency. We call them neutrosophic Armstrong’s axioms and are given as follows:

(A₁) α -nfd reflexive rule

If $Y \subseteq X \subseteq R$, then $X \xrightarrow[\alpha]{nfd} Y$

(A₂) α -nfd augmentation rule

If $X \xrightarrow[\alpha]{nfd} Y$ and $Z \subseteq R$ then $XZ \xrightarrow[\alpha]{nfd} YZ$

(A₃) α -nfd transitive rule

If $X \xrightarrow[\alpha_1]{nfd} Y$, $X \xrightarrow[\alpha_2]{nfd} Y$ then $X \xrightarrow[\min(\alpha_1, \alpha_2)]{nfd} Z$

Theorem 1: Neutrosophic Armstrong’s axioms (A₁) - (A₃) are sound.

Proof:

(A₁) α -nfd reflexive rule: If $Y \subseteq X \subseteq R$, then $X \xrightarrow[\alpha]{nfd} Y$

Let $t_1[X](NE)_\alpha t_2[X]$ is true, i.e., $SE(t_1[X_i], t_2[X_i]) \geq \alpha \forall X_i \in X$.

Then, $SE(t_1[X_i], t_2[X_i]) \geq \alpha \forall X_i \in Y$ holds i.e.,

$t_1[Y](NE)_\alpha t_2[Y]$ is also true.

This implies $X \xrightarrow[\alpha]{nfd} Y$ holds. Hence proved

(A₂) α -nfd augmentation rule

If $X \xrightarrow[\alpha]{nfd} Y$ and $Z \subseteq R$ then $XZ \xrightarrow[\alpha]{nfd} YZ$

Let $X \xrightarrow[\alpha]{nfd} Y$

Now, from Definition 3.3, for any two tuples t_1 and t_2 if $t_1[X](NE)_\alpha t_2[X] \dots (1)$ is true,

then $t_1[Y](NE)_\alpha t_2[Y] \dots (2)$ is also true. Next, suppose

$t_1[XZ](NE)_\alpha t_2[XZ] \dots (3)$ is true. This

implies,

$$SE(t_1[X_i], t_2[X_i]) \geq \alpha, \forall X_i \in XZ$$

$$SE(t_1[X_i], t_2[X_i]) \geq \alpha, \forall X_i \in X \text{ and}$$

$$SE(t_1[X_i], t_2[X_i]) \geq \alpha, \forall X_i \in Z$$

$$\text{now } SE(t_1[X_i], t_2[X_i]) \geq \alpha$$

$$, \forall X_i \in Z \Rightarrow$$

$$t_1[Z](NE)_\alpha t_2[Z] \dots (4)$$

Then from (2) and (4), we get

$$t_1 [YZ](NE)_{\alpha} t_2 [YZ] \dots\dots\dots(5)$$

Thus, for any two tuples t_1 and t_2 if $t_1[XZ](NE)_{\alpha} t_2[XZ]$ then it is also the case that $t_1[YZ](NE)_{\alpha} t_2[YZ]$ which implies $XZ \xrightarrow{\alpha} YZ$. Hence proved.

(A3) α -nfd transitive rule

$$\text{If } X \xrightarrow{\alpha_1} Y, X \xrightarrow{\alpha_2} Y \text{ then}$$

$$X \xrightarrow{\min(\alpha_1, \alpha_2)} Z$$

Let us assume that both the nfd's $X \xrightarrow{\alpha_1} Y, Y \xrightarrow{\alpha_2} Z$ hold in the relation $r(R)$.

Case I

$\alpha_1 \geq \alpha_2$ so that $\min(\alpha_1, \alpha_2) = \alpha_2$.

Given that $X \xrightarrow{\alpha_1} Y$ and $0 \leq \alpha_2 \leq \alpha_1 \leq 1$.

So, using

Proposition 2: we get $X \xrightarrow{\alpha_2} Y$ ----- (1)

Then, from (i) we can write

$$t_1[X](NE)_{\alpha_2} t_2[X] \Rightarrow t_1[Y](NE)_{\alpha_2} t_2[Y] \dots\dots(2)$$

Again, since $Y \xrightarrow{\alpha_2} Z$ holds, so we have

$$t_1[Y](NE)_{\alpha_2} t_2[Y] \Rightarrow t_1[Z](NE)_{\alpha_2} t_2[Z] \dots\dots(3)$$

Combining (2) and (3), we get

$$t_1[X](NE)_{\alpha_2} t_2[X] \Rightarrow t_1[Z](NE)_{\alpha_2} t_2[Z] \text{ which implies}$$

$$X \xrightarrow{\alpha_2} Z$$

Hence for $\alpha_2 = \min(\alpha_1, \alpha_2)$, if $X \xrightarrow{\alpha_1} Y, Y \xrightarrow{\alpha_2} Z$ then

$$X \xrightarrow{\alpha_2} Z$$

Case II: $\alpha_2 \geq \alpha_1$ follows similarly. Hence proved.

Using the above neutrosophic Armstrong's axioms, the following results are also derived for α -nfd.

(A4) α -nfd decomposition rule

$$\text{If } X \xrightarrow{\alpha} YZ \text{ then } X \xrightarrow{\alpha} Y, X \xrightarrow{\alpha} Z$$

Proof: Given that $X \xrightarrow{\alpha} YZ$ (1)

By α -nfd reflexive rule, we have $YZ \xrightarrow{\alpha} Y$ -----(2)

From (1) and (2) using α -nfd transitive rule, we get

$$X \xrightarrow{\alpha} Y, X \xrightarrow{\alpha} Z \text{ also follows similarly.}$$

Hence Proved.

(A5) α -nfd union rule

$$\text{If } X \xrightarrow{\alpha_1} Y, X \xrightarrow{\alpha_2} Z \text{ then } X \xrightarrow{\min(\alpha_1, \alpha_2)} YZ$$

Proof:

$$\text{Given that } X \xrightarrow{\alpha_1} Y \text{ ----- (1) and } X \xrightarrow{\alpha_2} Z \text{ ----- (2)}$$

From (1) we may write $X \xrightarrow{\alpha_1} XY$ ----- (3)(using α -nfd augmentation rule).

Similarly, from (2) we can write $XY \xrightarrow{\alpha_2} YZ$ ----- (4).

Thus from (3) and (4) using α -nfd transitive rule, we get

$$X \xrightarrow{\min(\alpha_1, \alpha_2)} YZ \text{ .Hence proved.}$$

(A6) α -nfd pseudo transitive rule

If $X \xrightarrow{\alpha_1} Y$ and $WY \xrightarrow{\alpha_2} Z$ then

$$WX \xrightarrow{\min(\alpha_1, \alpha_2)} Z$$

Proof: Given that $X \xrightarrow{\alpha_1} Y$ (1) and

$$WY \xrightarrow{\alpha_2} Z \text{ ----- (2)}$$

From (1), using α -nfd augmentation rule we can write

$$WX \xrightarrow{\alpha_1} WY \text{ ----- (3)}$$

From (3) and (2) using α -nfd transitive rule, we get

$$WX \xrightarrow{\min(\alpha_1, \alpha_2)} Z \text{ . Hence proved.}$$

D. Partial Neutrosophic Functional Dependency

After validation of Armstrong's axioms in the neutrosophic environment with our present notion of α -nfd, let us define partial neutrosophic functional dependency (partial α -nfd) as follows:

Definition 4: Y is called partially vague functionally dependent on X at α -level of choice, i.e., $X \xrightarrow{\alpha} Y$ partially, if $X \xrightarrow{\alpha} Y$, hold and also there exists a non-empty set $X' \subset X$, such that, $X \xrightarrow{\alpha} Y$. The notation of partial α -nfd is needed to define neutrosophic key.

Example 3: Let the relational schema be $R=\{A, B, C, D, E\}$ and the set of nfd's Non R be given by

$$N = \{ABC \xrightarrow{0.75} D, AC \xrightarrow{0.8} D\}$$

Then it easily observed that the nfd $ABC \xrightarrow{0.75} D$ is a partial α -nfd.

E. Neutrosophic Key

In classical relational database, key is a special case of functional dependency. The concept of classical key in the neutrosophic environment to define neutrosophic key with α -level of choice where 0,1 is a choice parameter defined by the database designer. A formal definition of neutrosophic keys as follows:

Definition 5: Let $K \subseteq R_j$ and N be a set of nfd's for R_j . Then, K is called a neutrosophic key of R_j at α -level of choice

where 0, iff $K \xrightarrow{\alpha \text{ nfd}} R_1 \in N$ and $K \xrightarrow{\alpha \text{ nfd}} R_1$ is not a partial α -nfd.

Example 4: Let us assume a relation schema $R_I = (A_I, B_I, C_I, D_I)$ and a set of nfd's

$$N = \{A \xrightarrow{0.75 \text{ nfd}} B, A \xrightarrow{0.8 \text{ nfd}} C, A \xrightarrow{0.7 \text{ nfd}} D\} \text{ of } R_I.$$

Find a neutrosophic key of R_I .

Solution:

Given $A \xrightarrow{0.75 \text{ nfd}} B$ (1), $A \xrightarrow{0.8 \text{ nfd}} C$ (2),

$$A \xrightarrow{0.7 \text{ nfd}} D$$
(3)

Applying α -nfd union rule on (1) and (2), we get

$$A \xrightarrow{0.75 \text{ nfd}} BC$$
 (4)

Again, applying α -nfd union rule on (3) and (4), we get

$$A \xrightarrow{0.7 \text{ nfd}} BCD$$
 (5)

Also, $A \xrightarrow{1 \text{ nfd}} A$ is trivial ---- (6)

Thus from (5) and (6) using α -nfd union rule, we get

$$A \xrightarrow{0.7 \text{ nfd}} ABCD$$
 that is $A \xrightarrow{0.7 \text{ nfd}} R_1$ which

implies that A is a neutrosophic key of R_I at 0.7-level of choice.

IV. CONCLUSION

In this paper, we have shown an extension of the classical relational database model with the concepts of neutrosophic set theory, a generalized version of vague sets. We mainly focused on the study of functional dependency in neutrosophic relational database. For this purpose, we have introduced a new kind of neutrosophic functional dependency (called α -nfd) based on the idea of α -equality of tuples and similarity measure of neutrosophic sets. We also expressed the neutrosophic inference rules and defined partial α -nfd and neutrosophic key.

The work may be extended to study Multivalued Dependency and Normalization using α -nfd which constitute an important part of a relational database design.

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